

Mathematical Notations

$:=$	Symbol indicating different notations for a single object	2
\cup	Table fusion	3
$a \in A$	a belongs to set A	4
$A \subset B$	A is included in B	5
$A \supset B$	A includes B	6
$A \cap B$	Intersection of sets A and B	7
$A \cup B$	Union of sets A and B	8
$A \setminus B$	Complement of set B in set A	9
$(A \cup B) \setminus (A \cap B)$	Symmetric difference of sets A and B	10
f_i	Frequency of a modality	11
$ x $	Absolute value of number x	12
$x!$	Factorial of number x	13
$\binom{n}{p}$	Binomial coefficient: number of ways of picking p elements out of n	14
$\Gamma(\cdot)$	Gamma function	15
γ	Euler's constant	16
$\psi(\cdot)$	Digamma function	17
π	Number π	18
λ	Scalar number	19
$\mathcal{A}, \mathcal{B}, \mathcal{C} \dots$	Matrices	20
\mathcal{I}	Identity matrix	21
$n \times p$	Indicates the size of a matrix	22
\mathcal{A}^\top	Transpose of matrix \mathcal{A}	23
\mathcal{B}^{-1}	Inverse of matrix \mathcal{B}	24
$\overline{\mathcal{C}}$	Conjugate of complex matrix \mathcal{C}	25
$\mathbf{x} = (x_1, \dots, x_n)^\top$	Column vector	26
\mathbf{x}^\top	Transpose of vector \mathbf{x}	27
$\mathcal{A} \otimes \mathcal{B}$	Kronecker product of matrix \mathcal{A} with matrix \mathcal{B}	28
$vec(\mathcal{A})$	Vector resulting from the stacking of columns of matrix \mathcal{A}	29
$vech(\mathcal{A})$	Vector resulting from the stacking of columns of matrix \mathcal{A} , but excluding elements above the diagonal	30

\mathcal{A}^*	Adjunct matrix (conjugate transpose) of matrix \mathcal{A}	31
$\mathcal{A}^{1/2}$	Square root of matrix \mathcal{A}	32
$\mathbb{1}_{[A]}(x)$	Equals 1 if $x \in A$ and 0 otherwise	33
$[a, b]$	Interval of values between a and b	34
$\det(\mathcal{A})$	Determinant of matrix \mathcal{A}	35
$\Phi(\cdot)$	Cumulative distribution function of a standard normal random variable $\mathcal{N}(0, 1)$	36
$\dot{\mathcal{X}}$	Matrix given by centring the columns of matrix \mathcal{X}	37
$\mathbb{1}_n$	Vector $(1, \dots, 1)^\top$ of length n	38
X, Y	Non-random variables (descriptive statistics)	39
N	Population size	40
n	Sample size	41
$m_e := q_{1/2}$	Median	42
$PFC_X(\cdot)$	Value of the polygon of cumulative frequencies of X	43
μ_X	Expected value of random variable X , or population mean in descriptive statistics	44
q_p or x_p	Fractile (quantile) of order p of a variable	45
$q_{1/4}, q_{3/4}$	First and third quartiles (also noted q_1 and q_3)	46
$\sigma_{Pop}^2(\mathbf{x})$	Population variance (descriptive statistics)	47
$\sigma_{Pop}(\mathbf{x})$	Population standard error (descriptive statistics)	48
c_v	Population coefficient of variation (descriptive statistics)	49
γ_1	Skewness	50
β_2	Kurtosis	51
μ_3	Centred moment of order 3	52
μ_4	Centred moment of order 4	53
χ^2	Pearson's χ^2 statistic	54
Φ^2, V^2	Cramér's Φ^2 and V^2	55
τ, τ_b	Kendall's τ and τ_b	56
ρ	Theoretical Pearson coefficient of correlation	57
$\eta_{Y X}^2$	Correlation ratio	58
X, Y, ϵ	Random variables	59
x_i, y_i, ϵ_i	Realizations of random variables X, Y, ϵ	60
$\mathbf{X}, \mathbf{Y}, \boldsymbol{\epsilon}$	Random vectors	61
\mathbf{X}_n	Sample (random)	62
\mathbf{x}_n	Sample (observed)	63
\mathbf{X}	Random matrix	64
\mathcal{L}	Generic distribution of a random variable	65
$\mathcal{N}(0, 1)$	Standard normal distribution	66
$\mathcal{N}(\mu, \sigma^2)$	Normal distribution with mean μ and variance σ^2	67
$\mathcal{U}(a, b)$	Uniform distribution over the interval $[a, b]$	68
$\text{Bin}(n, p)$	Binomial distribution with parameters n and p	69
$\mathcal{E}(\lambda)$	Exponential distribution with parameter λ	70

$\mathcal{P}(\lambda)$	Poisson distribution with parameter λ	71
$\mathcal{T}(n)$	Student distribution with n degrees of freedom	72
$\chi^2(n)$ or χ_n^2	χ^2 distribution with n degrees of freedom	73
$\mathcal{F}(n, m)$	Fisher distribution with n and m degrees of freedom	74
$f_X(\cdot)$	Probability density function of random variable X	75
$F_X(\cdot)$	Cumulative distribution function of random variable X	76
$F_X^{-1}(\cdot)$	Inverse cumulative distribution function of random variable X	77
μ	Expected value of a random variable	78
σ^2	Variance of a random variable	79
$\mathbb{E}(Y)$	Theoretical expectation of random variable Y	80
$\mathbb{V}\text{ar}(Y)$	Theoretical variance of random variable Y	81
\bar{X}_n	Empirical mean $\frac{1}{n} \sum_{i=1}^n X_i$ of sample $\mathbf{X}_n = (X_1, \dots, X_n)^\top$, estimator of μ_X	82
\bar{x}_n	Realization of the empirical mean $\frac{1}{n} \sum_{i=1}^n X_i$ of sample $\mathbf{X}_n = (X_1, \dots, X_n)^\top$, estimate of μ_X	83
\xrightarrow{P}	Convergence in probability	84
$\hat{F}_n(\cdot) := \hat{F}_{\mathbf{X}_n}(\cdot)$	Empirical cumulative distribution function of sample \mathbf{X}_n	85
θ	Unknown parameter (the true unknown value of the parameter will sometimes be noted θ^*)	86
$\hat{\theta}(X_1, \dots, X_n)$ or $\hat{\theta}$	Estimator of unknown parameter θ based on the sample $\mathbf{X}_n = (X_1, \dots, X_n)^\top$	87
$\hat{\theta}(x_1, \dots, x_n)$ or $\hat{\theta}$	Estimate of unknown parameter θ based on the observed sample $\mathbf{x}_n = (x_1, \dots, x_n)^\top$	88
$\mathbb{B}(\hat{\theta}(X_1, \dots, X_n); \theta)$	Bias of estimator $\hat{\theta}(X_1, \dots, X_n)$ to estimate unknown parameter θ	89
$P[A]$	Probability of set A	90
$\mathcal{V}(\theta; X_1, \dots, X_n)$	Likelihood function of sample \mathbf{X}_n evaluated at θ	91
$\mathbf{x}^* = (x_1^*, \dots, x_n^*)^\top$	Bootstrap sample generated from the observed sample $\mathbf{x}_n = (x_1, \dots, x_n)^\top$	92
$\hat{\sigma}$	Estimator of σ	93
$\hat{\sigma}$	Estimate of σ	94
p	Proportion	95
\hat{p}	Estimator of a proportion (or of a probability)	96
\hat{p}	Estimate of a proportion (or of a probability)	97
\widehat{m}_e	Estimator of a median	98
\widehat{m}_e	Estimate of a median	99
M	Number of iterations (of generated samples) in a Monte Carlo simulation	100
B	Number of generated bootstrap samples	101
$B(\cdot, \cdot), \Gamma(\cdot)$	Beta function, gamma function	102
$I'_x(\cdot, \cdot)$	Derivative of incomplete beta function	103

$I(\cdot)$	Modified Bessel function	104
$I_\alpha(\cdot)$	Modified Bessel functions	105
u_p	Quantile of order p of a $\mathcal{N}(0, 1)$	106
t_p^n	Quantile of order p of a $\mathcal{T}(n)$	107
q_p^n	Quantile of order p of a $\chi^2(n)$	108
$f_p^{n,m}$	Quantile of order p of a $\mathcal{F}(n, m)$	109
$CI_{1-\alpha}(\theta)$	Random confidence interval at confidence level $1 - \alpha$ for θ	110
$ci_{1-\alpha}(\theta)$	Realized confidence interval at confidence level $1 - \alpha$ for θ	111
$1 - \alpha$	Level of a confidence interval	112
$(x_{(1)}, \dots, x_{(n)})$	Observed sample, sorted from smallest to largest value	113
\mathcal{H}_1	Assertion of interest in hypothesis testing	114
\mathcal{H}_0	“Null” hypothesis, opposite of \mathcal{H}_1	115
α	Significance level or risk of the first kind in hypothesis testing	116
R	Random Pearson empirical coefficient of correlation	117
r	Realized Pearson empirical coefficient of correlation	118
β_0, β_1	Unknown coefficients of a simple linear regression model	119
$\hat{\beta}_0, \hat{\beta}_1$	Estimates of unknown coefficients of a simple linear regression model	120
$\hat{\epsilon}_i$	Observed residuals in a simple linear regression model	121
\hat{y}_i	Adjusted observed values in a simple linear regression model	122
R^2	Random coefficient of determination in regression	123
r^2	Realized coefficient of determination in regression	124
R_a^2	Random adjusted coefficient of determination in regression	125
r_a^2	Realized adjusted coefficient of determination in regression	126
\hat{Y}^p	Predictor of random variable Y for a new value of the explanatory variable X in regression	127
$PI_{1-\alpha}(Y_0, x_0)$	Prediction interval at level $1 - \alpha$ for random variable Y_0 associated with a new value x_0 of the explanatory variable	128
$\beta = (\beta_0, \dots, \beta_p)^\top$	Vector of the $p + 1$ unknown coefficients in a multiple linear regression model with p explanatory variables	129
$\hat{\beta} = (\mathcal{X}^\top \mathcal{X})^{-1} \mathcal{X}^\top \mathbf{Y}$	Estimator of the vector of unknown parameters β for the matrix \mathcal{X} of observed explanatory variables and for the observed vector of explained values in a multiple linear regression model	130
$\hat{\beta}$	Estimate of β	131
VIF	Variance inflation factor	132
AIC	An Information Criterion	133
BIC	Bayesian information criterion	134
h_{ii}	Leverage of i th observation in regression	135
t_i	Standardized residuals	136
t_i^*	Studentized residuals	137
$\hat{\sigma}_{(-i)}$	Estimate of σ excluding i th observation	138

C_i	Cook's distances	139
$\hat{y}_j^{(-i)}$	Prediction of y_j , not using the i th observation	140
$\hat{\beta}_j^{(-i)}$	Estimate of β_j , not using the i th observation	141
I, J	Number of levels of a factor in ANOVA	142
$\mu_{\bullet\bullet}$	Mean general effect in ANOVA	143
$\mu_{i\bullet}$	Effect of level i of a factor in ANOVA	144
$\mu_{\bullet j}$	Effect of level j of a factor in ANOVA	145

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